

# 分子結晶における電荷秩序の融解と超伝導に関する 密度行列繰り込み群による研究

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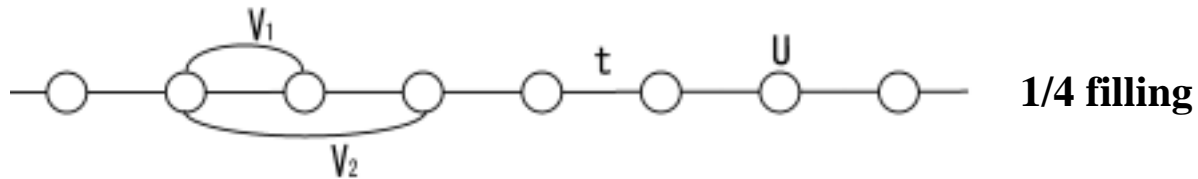
1. Extended Hubbard model on **a single chain (TMTTF)**
2. Extended Hubbard model on **a double chain (spin-gap liquid)**
3. Extended Hubbard ( $t$ - $J$ ) model on the **anisotropic triangular lattice (superconducting correlations)**
4. Future directions

**Melting of CO due to charge frustration,  
leading to anomalous metallic states.  
DMRG method**

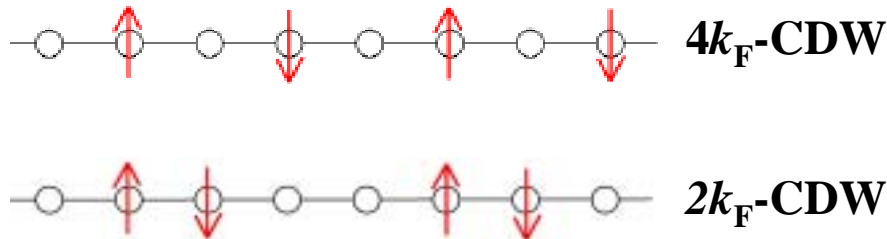
# Extended Hubbard model on a single chain

**Melting of CO** due to charge frustration

Precise determination of the **ground-state phase diagram** and  $K_\rho$

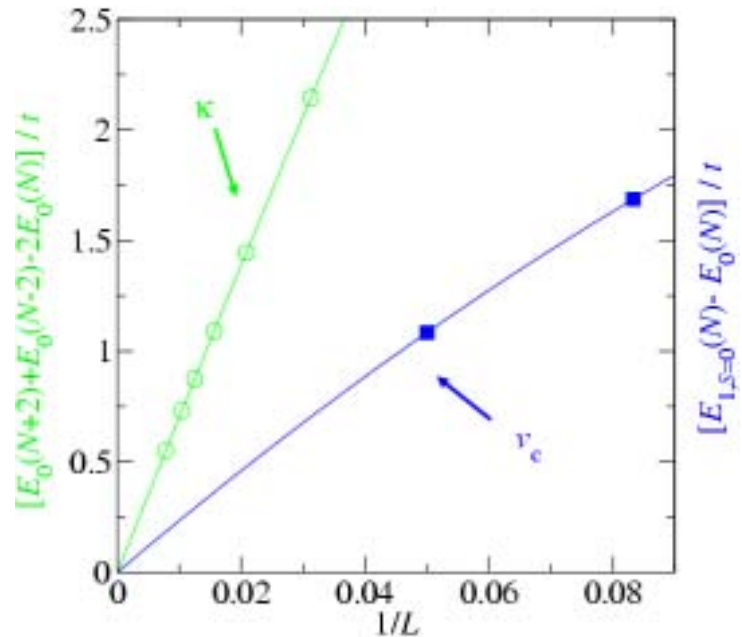


**CO patterns** at quarter filling

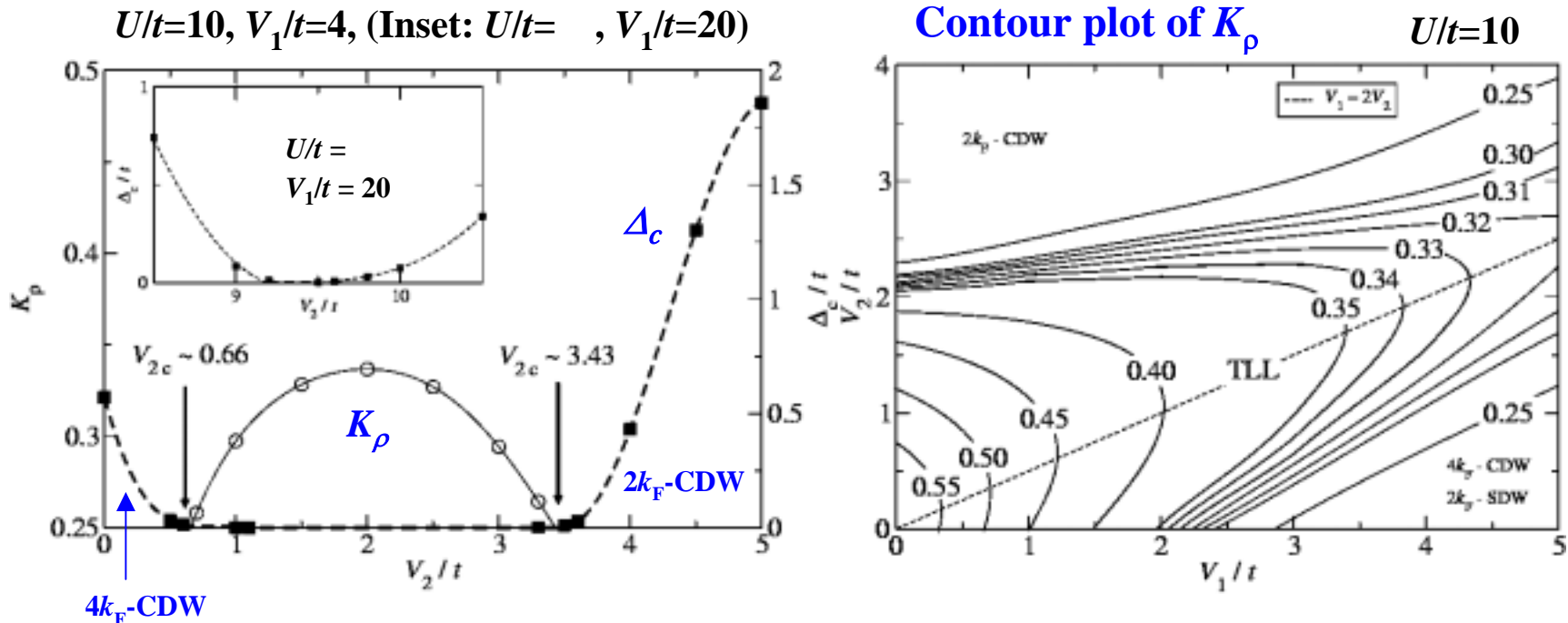


$K_\rho$  is determined from **compressibility  $\kappa$  (DMRG)** and **charge velocity  $v_c$  (ED)**.

DMRG method: up to 128 sites,  
 $m=500$ ,  $\delta E < 1.0 \times 10^{-4} t$



# Ground-state phase diagram and $K_\rho$



**TLL always with  $K_\rho > 0.25$ .**

**Charge gap opens and CDW occurs at  $K_\rho=0.25$ .**

**Experiment:**

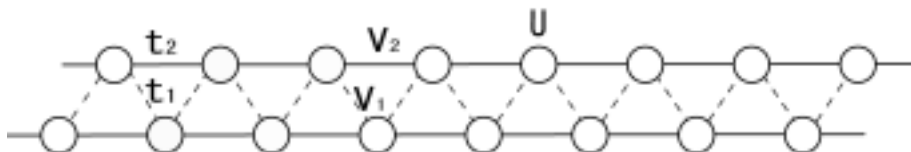
**TMTSF:  $K_\rho = 0.23$**  (Schwartz *et al.*: PRB 58, 1261 (1998))

**TTF-TCNQ:  $K_\rho = 0.17$**  (Sing *et al.*: PRB 68, 125111 (2003))

**$U$ -independent. Filling dependence?**

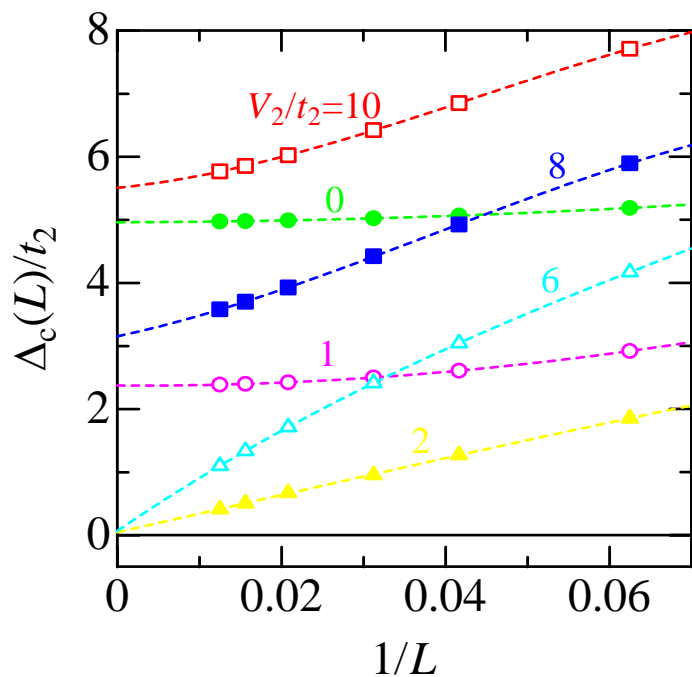
# Double-chain Hubbard model

S. Nishimoto and Y.O.: PRB 68 (2003) 235114.

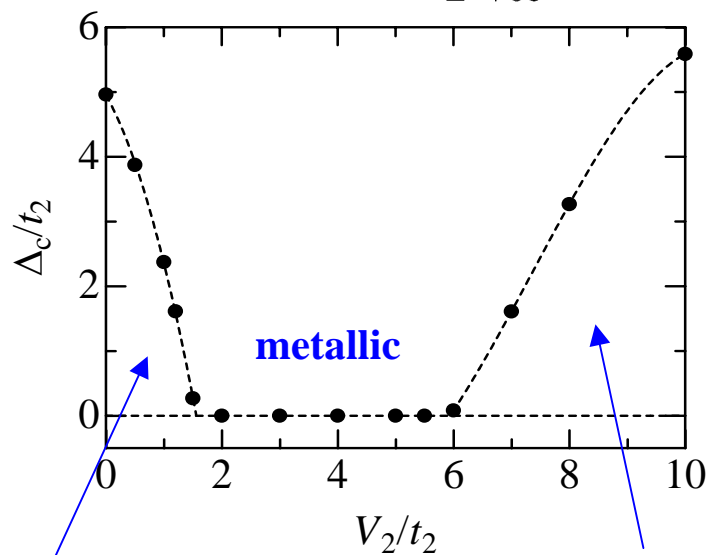


CuO double chains of nonsuperconducting  $\text{PrBa}_2\text{Cu}_4\text{O}_8$

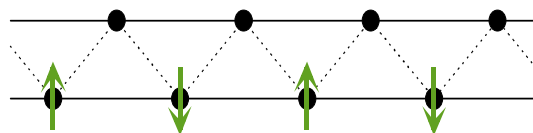
$t_2 \gg t_1$ ,  $U/t_2=20$ ,  $V_1/t_2=5$ , quarter filling



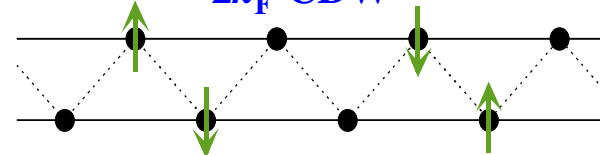
$$\Delta_c = \lim_{L \rightarrow \infty} \Delta_c(L)$$



$4k_F$ -CDW



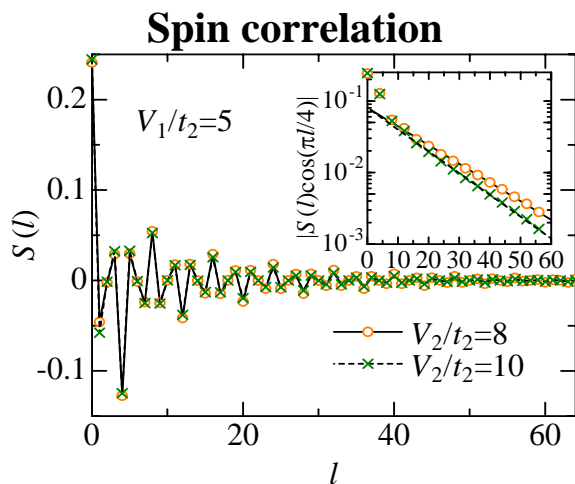
$2k_F$ -CDW



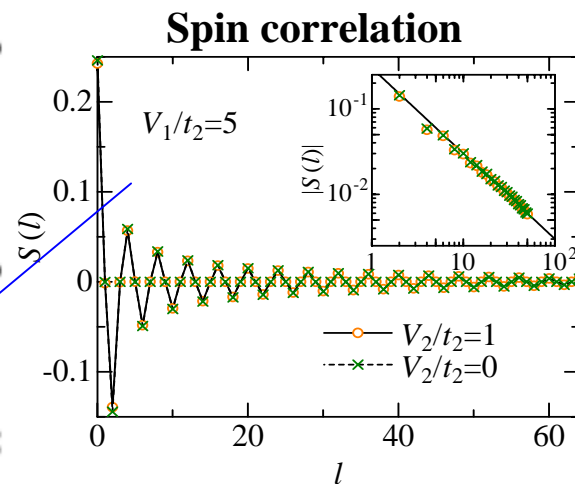
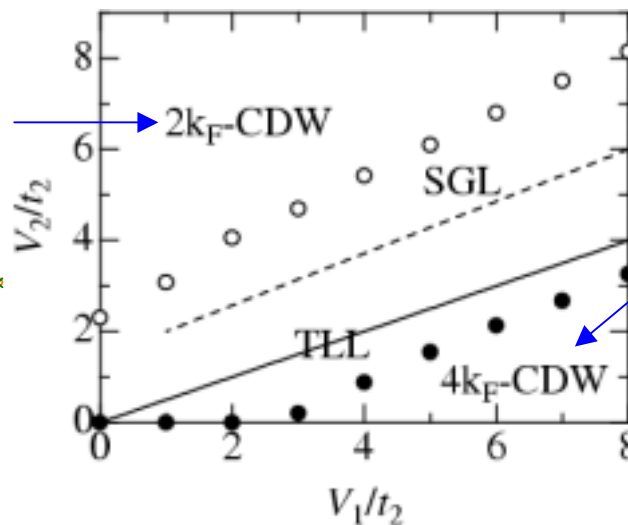
# Ground-state phase diagram

S. Nishimoto and Y.O.: PRB 68 (2003) 235114

## Presence of spin-gap liquid phase



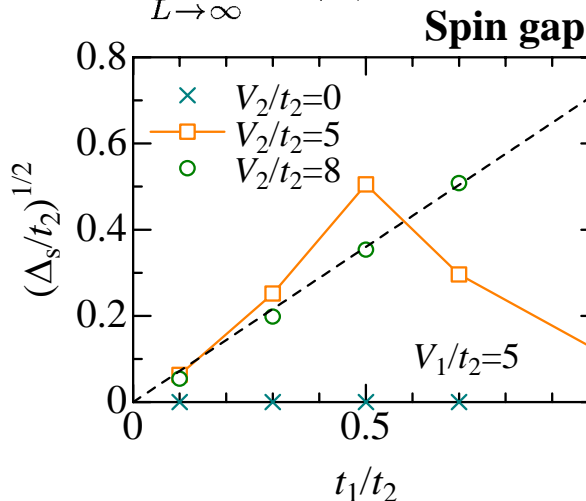
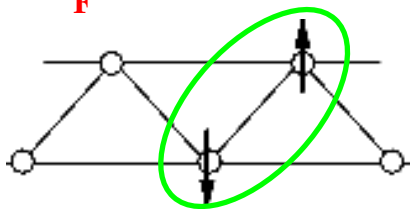
**Exponential decay**  
**Heisenberg ladder**



**Power-low decay**  
**Heisenberg chain**

$$\Delta_s = \lim_{L \rightarrow \infty} \Delta_s(L)$$

$\Delta_s \propto t_1^2$   
**near  $2k_F$ -CDW**

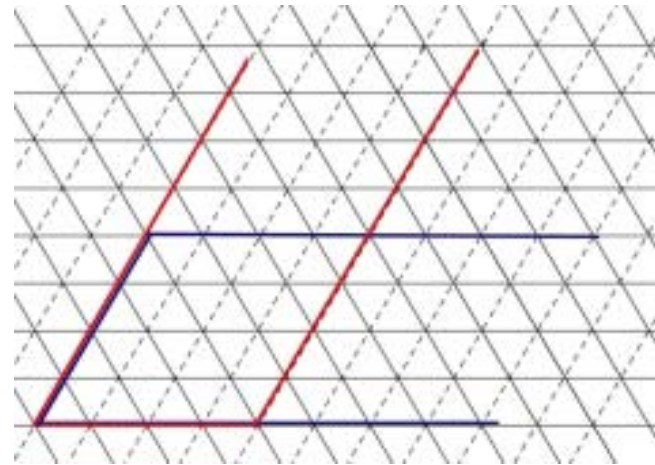
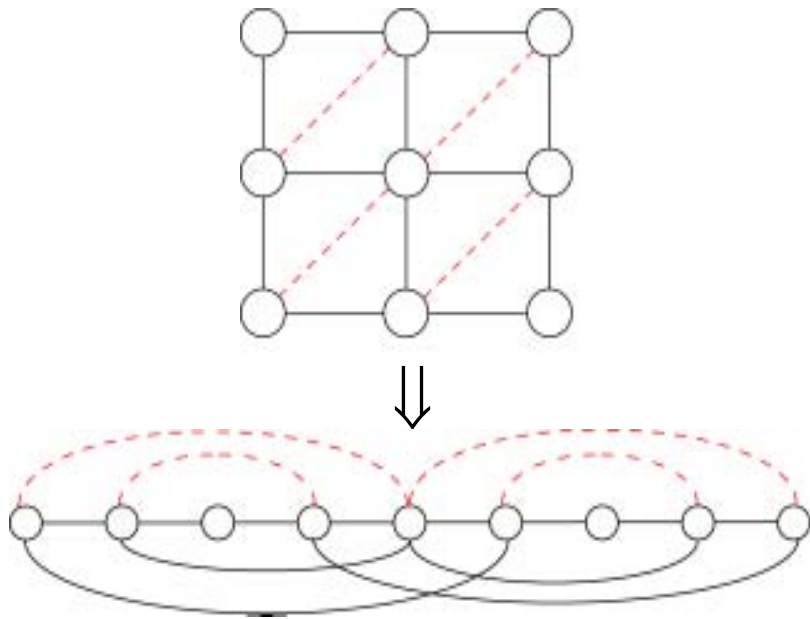


**Mobile  
singlet pairs**

# Anisotropic triangular lattices

Is DMRG applicable to 2D models?

Mapping to the 1D system with long-range interactions

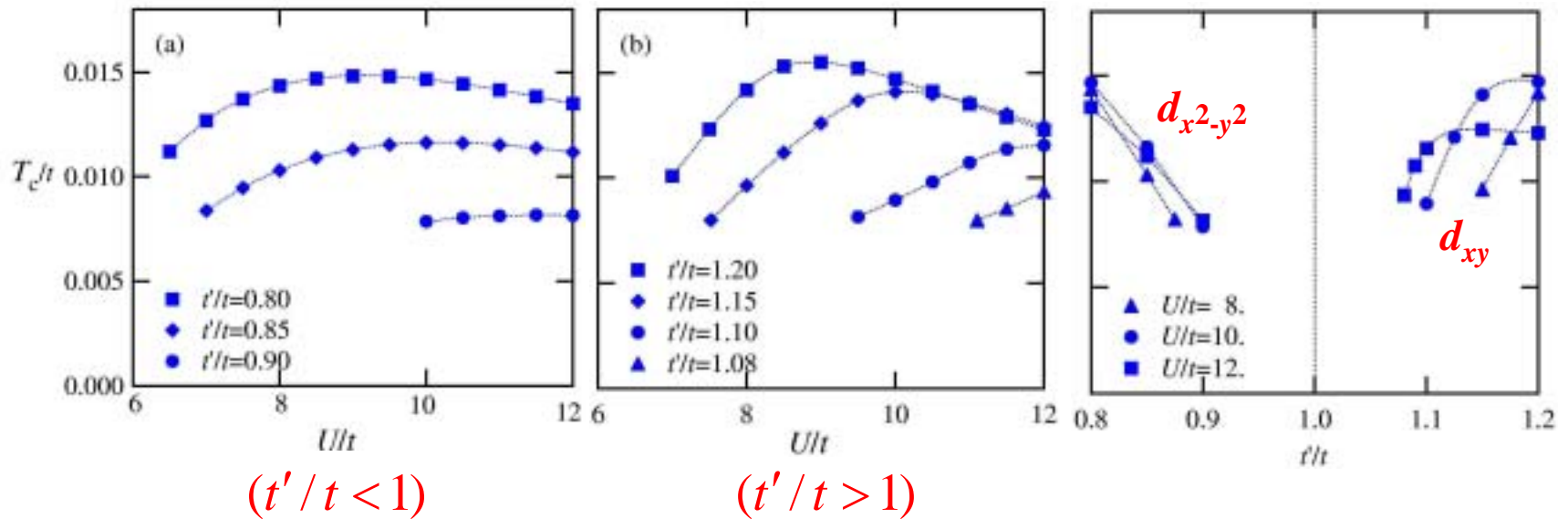


e.g.:  $24 \times 4$  cluster,  $m=1600$

We can use the **standard** DMRG method in 1D.

# FLEX approximation for the $t$ - $t'$ - $U$ Hubbard model at half filling

H. Kondo and T. Moriya: JPSJ 73 (2004) 812



$\Rightarrow$  Symmetry of order parameters changes  
from  $t'/t < 1$  to  $t'/t > 1$ ;  $d_{x^2-y^2} \Rightarrow d_{xy}$

# SC order parameters

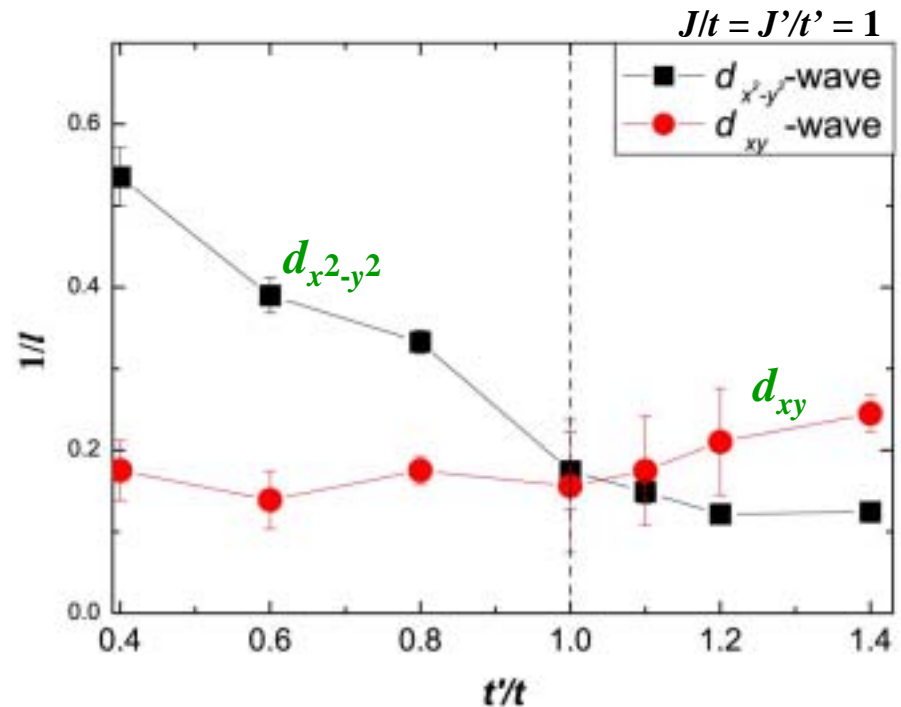
Anisotropic triangular-lattice  
 $t$ - $J$  model at  $n = 0.83$ .

We assume

$$\langle \Psi | \begin{matrix} x^2-y^2 \\ i \end{matrix} ( \begin{matrix} x^2-y^2 \\ i+r \end{matrix} )^\dagger | \Psi \rangle \propto r^{-l}$$

$$\langle \Psi | \begin{matrix} xy \\ i \end{matrix} ( \begin{matrix} xy \\ i+r \end{matrix} )^\dagger | \Psi \rangle \propto r^{-l}$$

and evaluate the value  
of  $1/l$ .



**Symmetry of the SC correlations changes from  $d_{x^2-y^2}$  to  $d_{xy}$  as we go from  $t'/t < 1$  to  $t'/t > 1$ .**

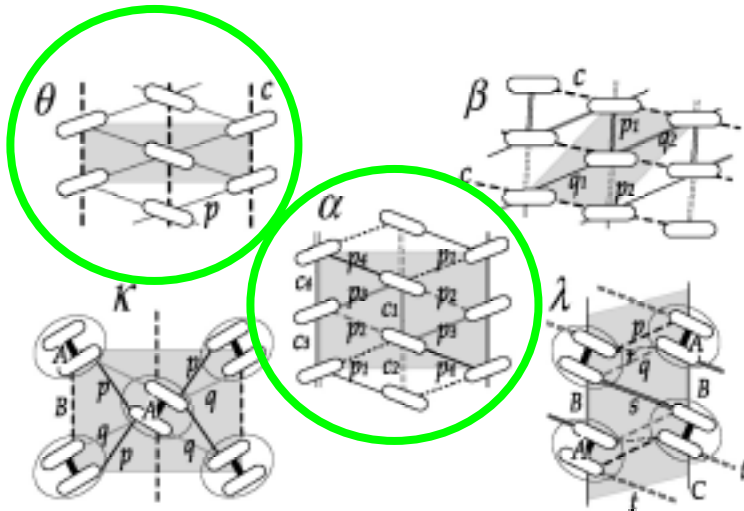


# Future directions

Extended Hubbard model at  $1/4$  filling  
on **the anisotropic triangular lattices**  
by **DMRG** method

$\theta$ -type  $(\text{BEDT-TTF})_2\text{X}$   
 $\alpha$ -type, etc.

**CO melting**  
**Charge fluctuations**  
**Mechanism of superconductivity**



C. Hotta: JPSJ: 72 (2003) 840.

